



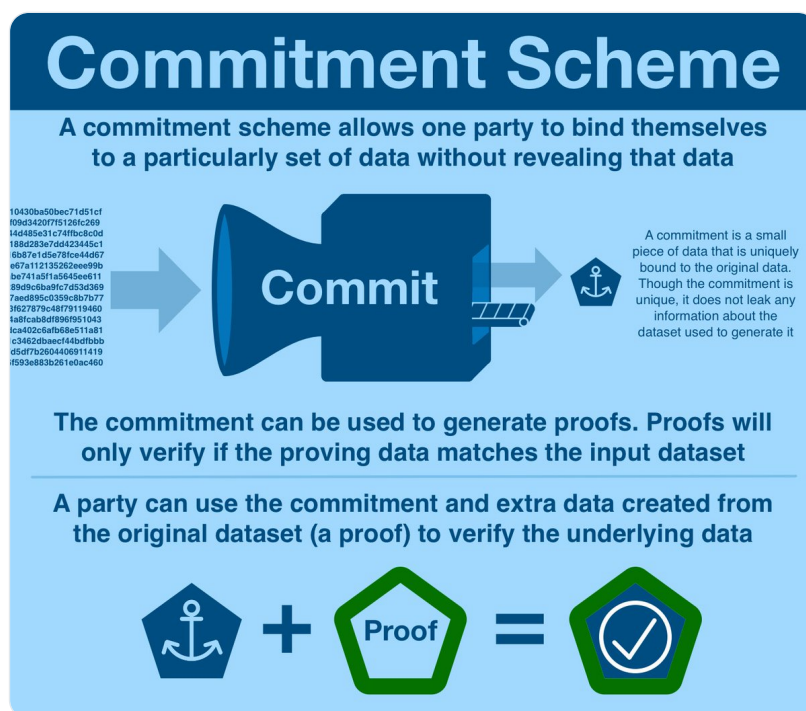
Haym @SalomonCrypto

Oct 30 · 21 tweets · [SalomonCrypto/status/1586809382813065216](https://twitter.com/SalomonCrypto/status/1586809382813065216)

(1/20) Cryptography Basics: Commitment Schemes

A commitment scheme is a primitive that allows one party to generate a piece of data anchored to a specific dataset.

This anchor (commitment), cannot leak information and yet can unequivocally verify the dataset.



(2/20) Let's say you have a large amount of data that, for whatever reason, is private.

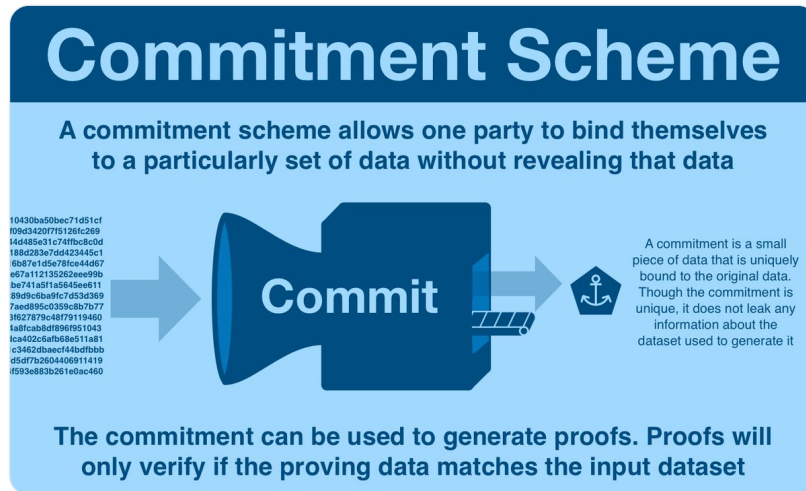
How can you provide a public audience assurance that you will not alter the data without allowing them to see it?

(3/20) The naive approach breaks our problem statement's basic privacy assumptions. Revealing the data allows public verification... at the cost of 100% of privacy.

We need to find a way to provide a unique fingerprint of that specific set of data to act as a signature.

(4/20) Here's the rough schematic of commitment generation:

- 0) start with data of arbitrary contents and size
- 1) feed data into a commitment scheme
- 2) commitment scheme generates a commitment, unique to a specific dataset



(5/20) The commitment is some unique piece of data that inseparably bound to the original dataset. Each dataset will generate a different commitment, and each commitment corresponds to a different dataset.

The trick: it is (almost) impossible to go from commitment → dataset.

(6/20) Because it is INCREDIBLY difficult to go from commitment to dataset, it can be publicly shared without any fear of leaking any of the underlying data.

If we stopped here, we'd still have something useful; digital fingerprints are just as useful as the IRL version.

(7/20) But we aren't going to stop here, a commitment scheme has a second act: the commitment can be opened!

We still cannot go from commitment to dataset; instead we can combine the commitment with a proof to verify the underlying data.



(8/20) Too abstract; let's run through some examples:

Alice is a patron of both BigBank and InsureCo and is processing a transaction that requires both. Instead of communicating it in public, BigBank and InsureCo commit to the same data and share commitments.

(9/20) Government worker Bob is distributing [thing] to eligible citizens, but can only identify people through sensitive information (eg a social security/national ID number). Bob shares a commitment to the dataset, which people can use to verify their eligibility.

(10/20) Charlie is building blocks for mev-boost. At auction, he can't reveal the block, else someone will just copy it and undercut him. Instead, he submits a commitment, binding him to a block that can be revealed if and only if it is chosen.



(11/20) In summary, the purpose of cryptographic commitment schemes is to publicly bind one party to a specific set of private data in a way that can be revealed later.

But not all commitment implementations are equal; some are more capable than others.

3 examples...

(12/20) Scheme 1 - Hashing

Commit: hash your dataset to generate a random-looking string

Open: reveal the data, making it available for others to hash

Verify: check the self-computed hash against the commitment

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(1/7) Computer Science 101: Hash Functions

What is a hash function? What are the characteristics of a good hash function? Where do hash functions appear and why do I hear about them all the time?

If you want to understand the fundamental tool of crypto, this guide is for you!

Hash Functions

A hash function transforms any amount of data into a compact value of uniform length.

INPUT	OUTPUT
Hello World	0x829bd824b016326a401d083b
Hello Wold	0xabd9bd33983cb06776e89273
Social Security Number: ****.***	0xad22b653d2d85490c0147dfa1
	0x91bfa44d98f1d3e2v2d098d5ff
	0x299dce9763c53debb12a87e1

A good hash function is quick and efficient to compute, but difficult (if not impossible) run in reverse, and distribute values uniformly (randomly) across all possible outputs.

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(13/20) While this scheme checks all the boxes of being a commitment scheme, it isn't particularly useful.

Opening is an all-or-nothing prospect. Not only does this have (obvious) implications for privacy, it has pretty aggressive bandwidth assumptions.

(14/20) Scheme 2 - Merkle Trees

Commit: generate the tree by applying rounds of hashing between nodes until a single root is remaining

Open: provide a piece of data and the required inner nodes to self-compute the root

Verify: compare the self-computed root to the commitment

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(1/13) Computer Science 201: Merkle Trees and Merkle Proofs

If you want to understand @Bitcoin, @ethereum and blockchain technology, you need to learn:

- How a Merkle trees expresses a large dataset
- How a Merkle proof works
- Why a Markle tree is so efficient

Merkle Trees and Proofs

The diagram illustrates two Merkle tree structures. The left tree shows a full tree with a root node 'hash(h1h2h3h4)', two intermediate nodes 'hash(h1h2)' and 'hash(h3h4)', and four leaf nodes 'hash(d1)', 'hash(d2)', 'hash(d3)', and 'hash(d4)', each pointing to data items 'data_1', 'data_2', 'data_3', and 'data_4'. The right tree shows a partial tree with the same root and intermediate nodes, but only the leaf nodes 'hash(d1)' and 'hash(d2)' are present, pointing to 'data_1' and 'data_2'. Labels 'provided' and 'computed' are placed above the intermediate nodes in the right tree to indicate the proof path.

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(15/20) In comparison to a simple hash-based scheme, Merkle trees are an enormous improvement.

First, the commitment can be opened privately at an individual point. The opener will need the inner nodes, but those can be shared without leaking any data in the underlying dataset.

(16/20) Second, the Merkle trees are MUCH more efficient than a hash-based scheme. Instead of transmitting the entire dataset, Merkle proofs require $O(\log n)$.

For those of you with a life, $O(\log n)$ just means the proof size grows exponentially slower than the dataset size.

(17/20) Quick aside, while Merkle trees are a huge improvement, they are not perfect.

This $O(\log n)$ idea is a double-edged sword. Yes, it does grow slower than the dataset, but it will grow, relentless and unceasingly.



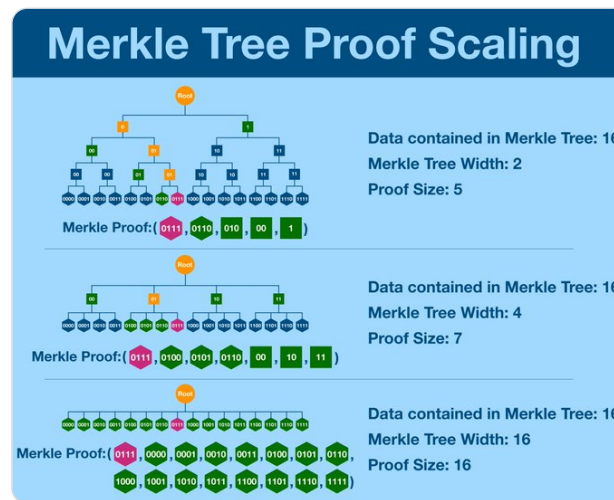
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(1/18) The Problem with Merkle Trees

At the heart of @Bitcoin, @ethereum and many blockchain computers is the Merkle Tree. While this data structure has served us well, it is not perfect... and if you look ahead, you can see impending problems.

Let's talk Merkle proof scaling.



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(18/20) Scheme 3 - KZG Polynomial Commitments

KZG Commitments (also called Kate Commitments) are a little too complex to break down into one tweet. Instead, check out this thread.

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(1/24) KZG Polynomial Commitments: The Complete Guide

Our goal: 1) prove we are committed to a specific set of data and 2) allow others to verify specific points within that dataset.

Want to see some mathematical magic? This megathread is for you!

KZG Commitment Scheme

First, the prover commits to data by creating a point on the elliptic curve. If the data changes, the prover cannot create valid proofs.

Prover

- 1) Commit
- 3) Proof Evaluation

Verifier

- 2) Request

Next, the verifier gives a data point. The prover builds a new elliptic curve point and a polynomial evaluation around that point.

KZG Proof Verification

$$e([S - z], [h(S)]) \stackrel{?}{=} e([f(S) - f(z), [1]])$$

↓

$$e([S - z], [Z]) \stackrel{?}{=} e([\text{Anchor}] - f(z), [1])$$

Calculated by verifierProofCommitEvaluation

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(19/20) TL;dr KZG commitments allow a party to commit to a dataset in a way that can be opened at any point. However, unlike Merkle trees, KZG commitments have a constant proof size.

You can prove any amount of evaluations (think millions) with just one 48 byte piece of data!

(20/20) By now, you've definitely got it. A commitment scheme is about creating commitment that is anchored to a piece of data. Schemes that can be opened at specific points are particularly useful; the questions are just of commitment calculation efficiency and proof size.

More of a long form reader? Try this out:



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Commitment Schemes

Commitment Schemes | Haym

(1/20) Cryptography Basics: Commitment Schemes A commitment scheme is a primitive that allows one party to generate a piece of data anchored to a specific dataset. This anchor (commitment), cannot ...

<https://typefully.com/SalomonCrypto/NEIAXC8>

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(1/20) Cryptography Basics: Commitment Schemes

A commitment scheme is a primitive that allows one party to generate a piece of data anchored to a specific dataset.

This anchor (commitment), cannot leak information and yet can unequivocally verify the dataset.

Commitment Scheme

A commitment scheme allows one party to bind themselves to a particularly set of data without revealing that data

Commit

A commitment is a small piece of data that is uniquely bound to the original data. Though the commitment is unique, it does not leak any information about the dataset used to generate it

The commitment can be used to generate proofs. Proofs will only verify if the proving data matches the input dataset

A party can use the commitment and extra data created from the original dataset (a proof) to verify the underlying data

+ =

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